

Work and energy

Work energy theorem

$$\text{Work} = \Delta KE$$

Work = change in kinetic Energy

$$\frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2$$

$$\frac{1}{2}m(v_f^2 - v_i^2) \neq \frac{1}{2}m(v_f - v_i)^2$$

To change velocity, you have to have an acceleration (+/-),
In order to have an acceleration,

Newton's second Law tells us you have a net Force, & if you have a net Force, & some displacement, you are doing work or work is being done.

Conservation of Energy

Energy can not be created or destroyed in a closed system, it can only change forms.

⇒ Conservation of Mechanical Energy

For a closed system, with No external Forces acting on it, Mechanical Energy is conserved

$$ME_i = ME_f$$

$$PE_i + KE_i = PE_f + KE_f$$

$$U_i + k_i = U_f + k_f$$

$$\text{Total Potential + Kinetic}_{\text{initial}} = \text{Total Potential + Kinetic}_{\text{Final}}$$

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$PE = m(9.81)(45) = 441.45 \text{ (m) J}$ Total ME throughout
 $KE = 0$ Zero
 $PE = (m)(9.81)(40) = 392.4 \text{ m J}$
 $KE = 4905 \text{ m}$
 $4905 \text{ m} = \frac{1}{2} m v^2$
 $\sqrt{98.1} = v$
 $v = 9.9 \text{ m/s}$

$882.9 = v^2$ $KE = 441.45 \text{ (m) } = \frac{1}{2} m v^2$
 $v = \sqrt{882.9} = 29.7 \text{ m/s}$

At the bottom of the hill, the ski patrol clocks you going 20 m/s.

Q What happened?

a. There was work done by friction (snow resistance + air resistance, friction)

Q. How much?

$E = 441.45 \text{ (m) J}$
 at bottom of hill $PE = 0$
 $KE = \frac{1}{2} m (20)^2 = 200 \text{ (m) J}$
 $W_{\text{by friction}} E_{\text{fr}} = 241.45 \text{ (m) J}$
 $= -241.45 \text{ (m) J}$

